

# Fraud Proofs

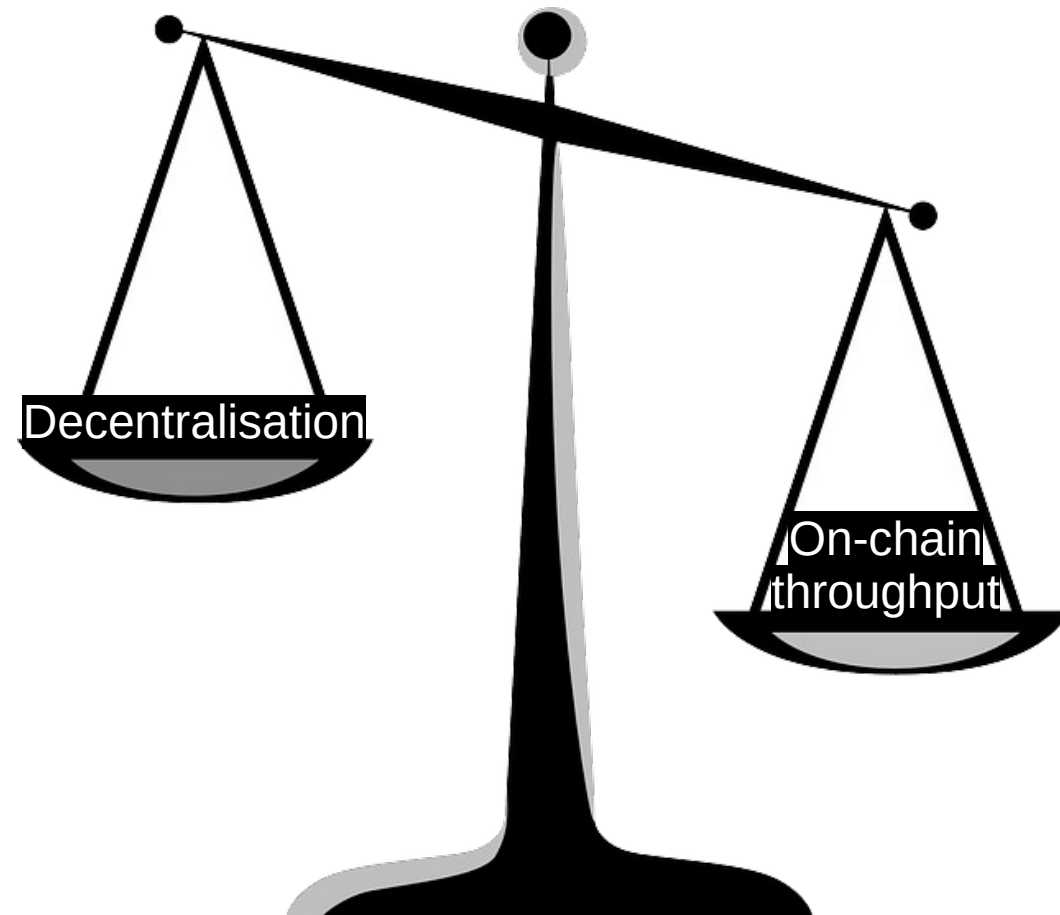
## Maximising SPV Security and Scaling Blockchains with Dishonest Majorities

Mustafa Al-Bassam

6 October 2018

# Motivation

- ▶ Currently there is a huge trade off between decentralisation and on-chain scalability.
- ▶ Because SPV nodes (non fully validating nodes) will accept invalid blocks.
  - ▶ They assume that the majority of the consensus is honest.



# Can we reduce this tradeoff?

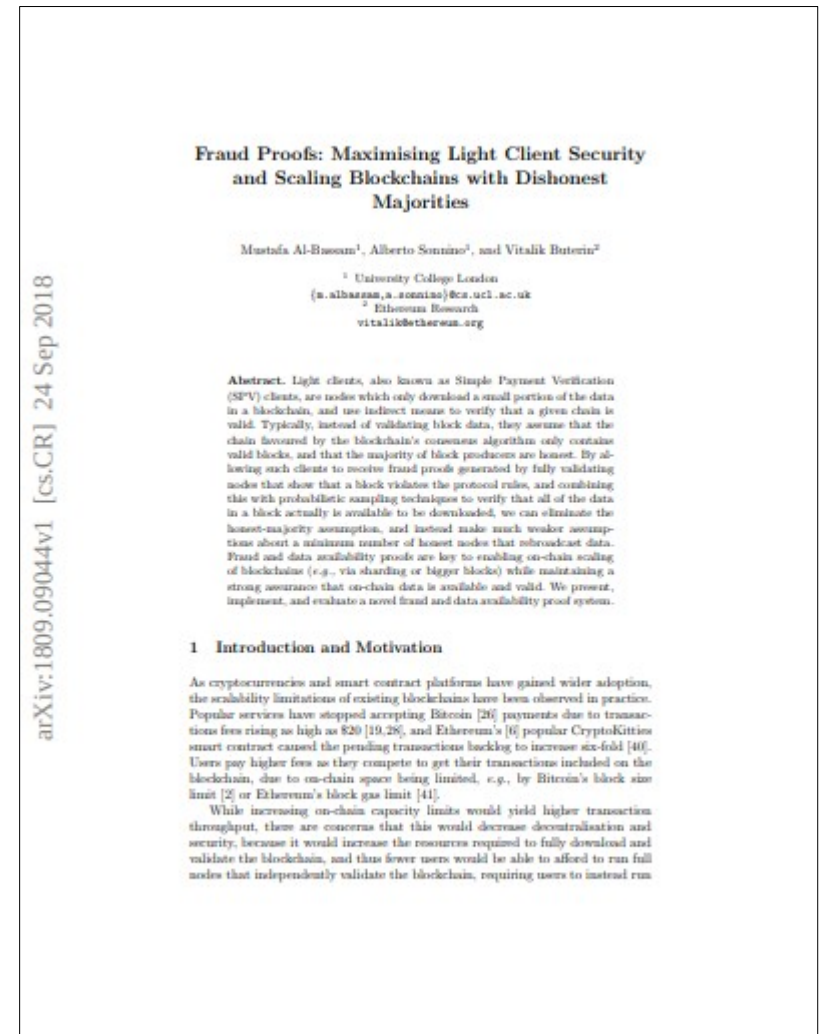
- ▶ The big question: how can we make non fully validating (SPV) nodes reject invalid blocks, so that they don't have to trust miners?
- ▶ Let's use fraud proofs and data availability proofs!

# Read the full paper (33 pages)

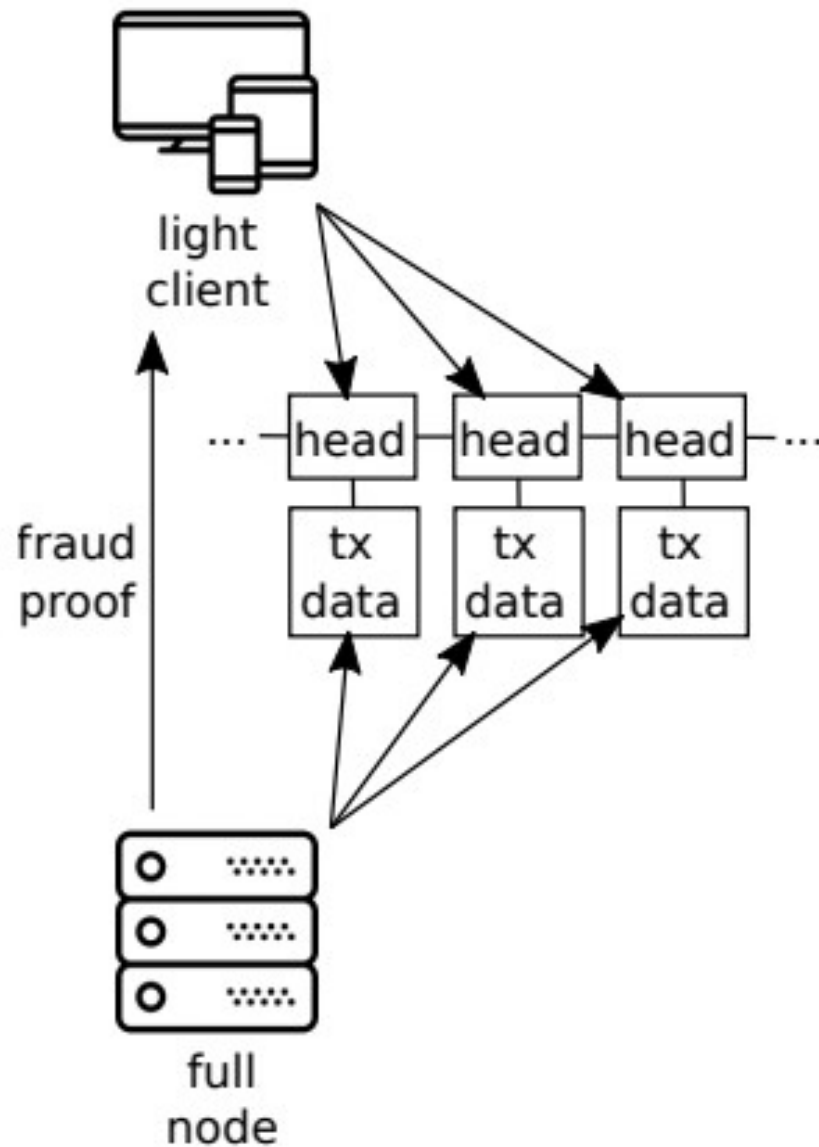
## ► Fraud Proofs: Maximising Light Client Security and Scaling Blockchains with Dishonest Majorities

Mustafa Al-Bassam, Alberto Sonnino, Vitalik Buterin

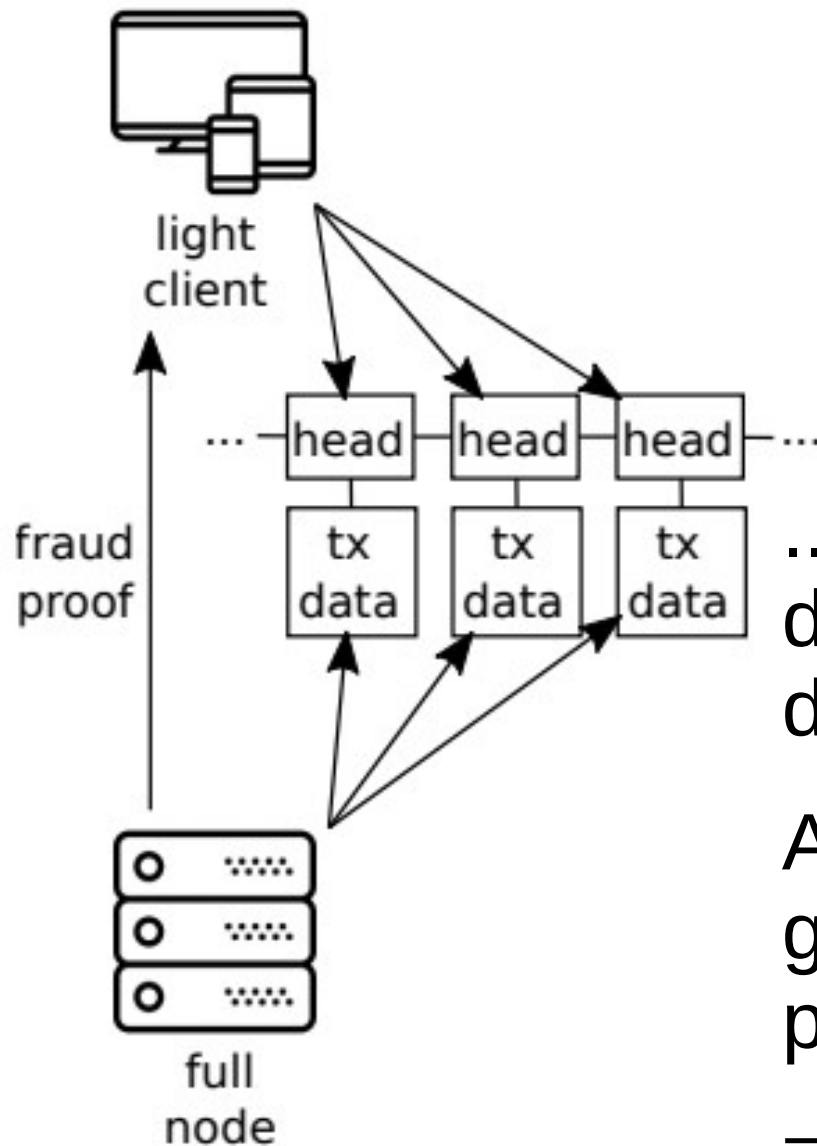
► <https://arxiv.org/abs/1809.09044>



# Fraud proofs: the basic idea



# Fraud proofs: the basic idea



...but what if the miner doesn't release the tx data?

A: Then we can't generate a fraud proof. 🤖

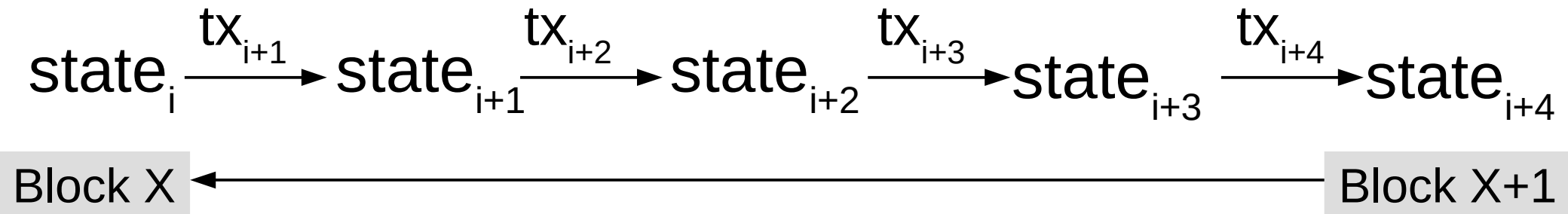
= We also need a way to guarantee data availability! 6

# Earlier discussion on fraud proofs

- ▶ The original Bitcoin whitepaper briefly mentions “alerts”; which are messages that full nodes can send to SPV clients to alert them the block is invalid. (Vulnerable to DoS.)
- ▶ G. Maxwell and P. Todd have done some work on “compact fraud proofs”. Early proposals require a different fraud proof for each way to violate the rules. We improve on this.
- ▶ G. Maxwell has discussed on IRC using erasure coding for data availability with a scheme using a “designated source” with PoW rate-limiting (and no way to deal with incorrectly generated codes?)

# Generalising the blockchain as a state transition system

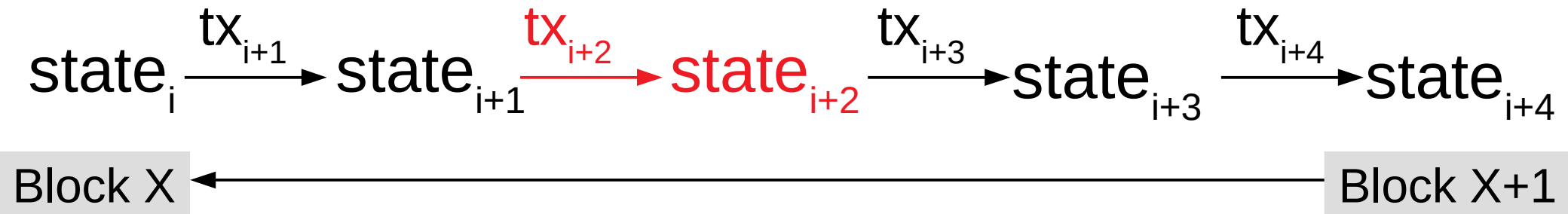
- ▶ Each transaction reads and modifies the state of the blockchain.
  - ▶  $\text{transition}(\text{state}, \text{tx}) = \text{state}'$  or *error*





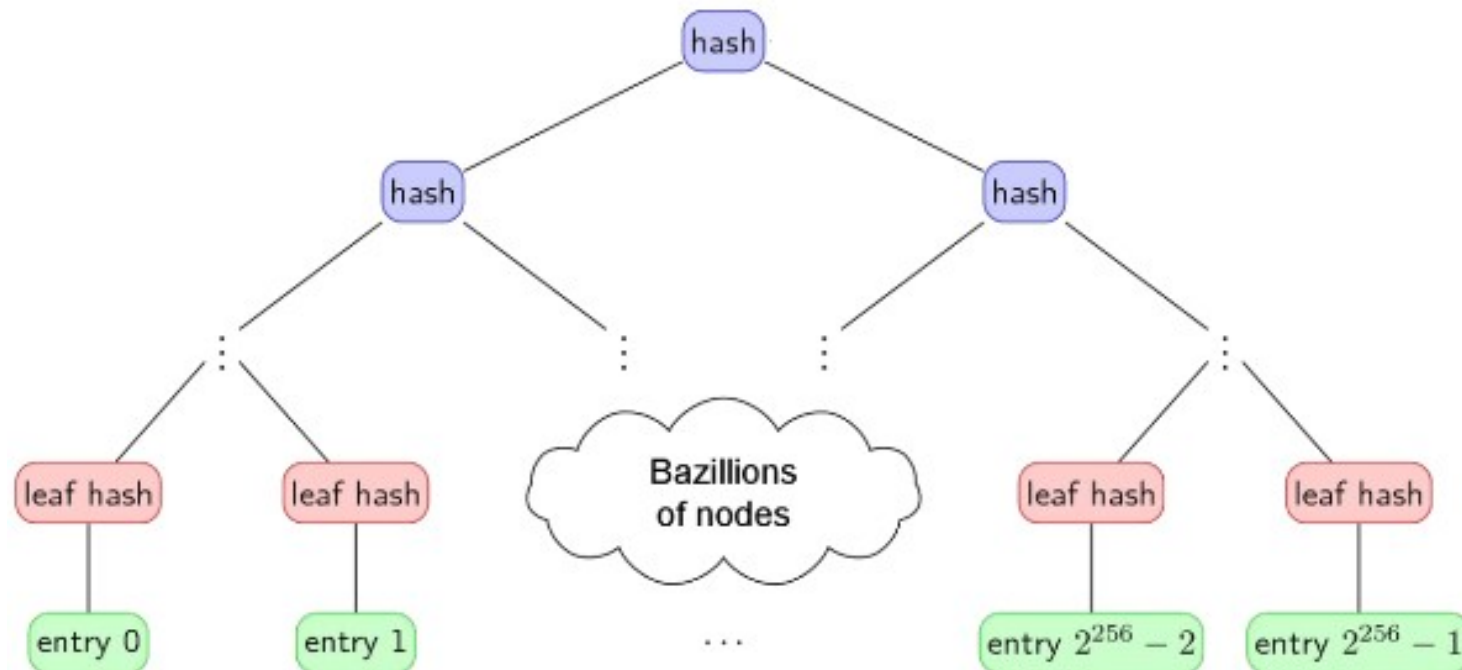
# Generalising the blockchain as a state transition system

- ▶ Each transaction reads and modifies the state of the blockchain.
  - ▶  $\text{transition}(\text{state}, \text{tx}) = \text{state}'$  or *error*
- ▶ But what if one of the transitions is erroneous?
  - ▶ We need a way to prove this.



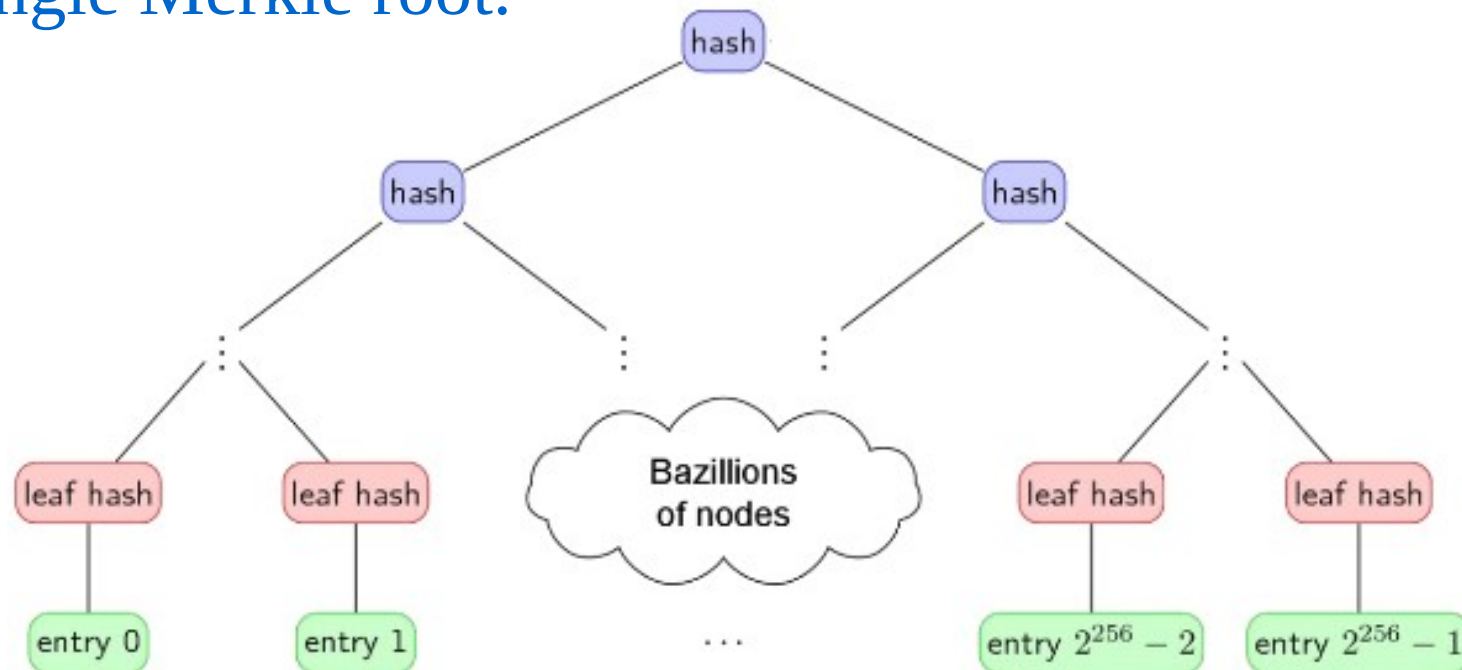
# Representing the entire state as a Merkle root

- ▶ We can store the state as a key-value store.
  - ▶ Key: UTXO ID. Value: 1 if unspent, 0 otherwise.
- ▶ We can use a Sparse Merkle tree to do this.
  - ▶ A tree with  $2^{256}$  leaves (every possible SHA-256 hash).



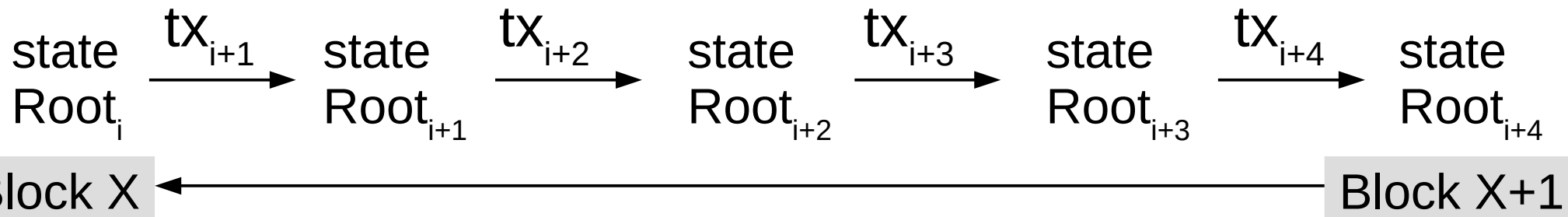
# Representing the entire state as a Merkle root

- ▶ Merkle proofs are still  $O(\log(n))$  as most branches will only contain leaves with default values (0).
- ▶ To access key  $K$  in the tree, access the  $hash(K)$ th item.
- ▶ We can thus represent the entire state of the blockchain as a single Merkle root.



# Generalising the blockchain as a state transition system

- ▶ Each transaction changes the state root of the blockchain.
  - ▶  $\text{transitionRoot}(\text{stateRoot}, \text{tx}, \text{witnesses}) = \text{stateRoot}'$  or *error*
  - ▶ The witnesses of a transaction are Merkle proofs of all the parts of the state the transactions accesses.
- ▶ **Execution trace:** we need to include the post-state root of transactions in the block. (e.g. every few transactions)



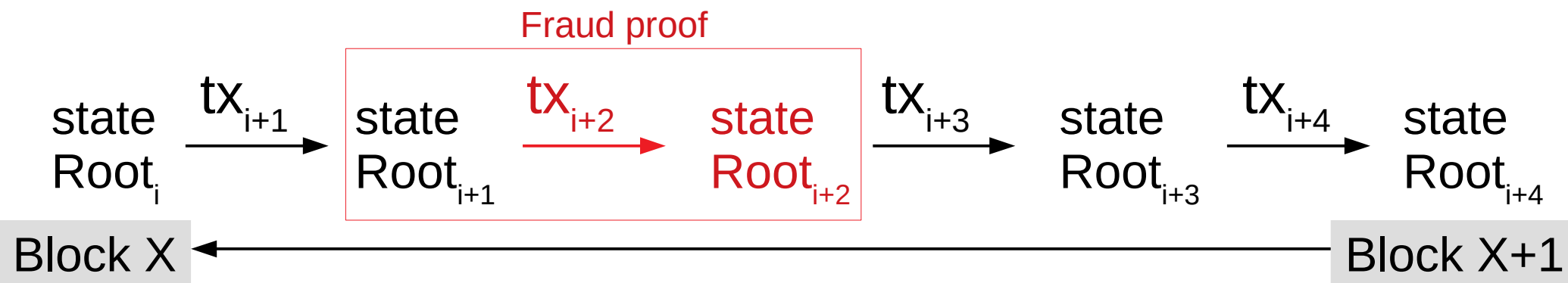
# Generalising the blockchain as a state transition system

- ▶ The fraud proof consists of the transaction and its pre-state root, post-state root, witnesses (+ Merkle proofs).

- ▶ If the Merkle proofs are valid, and

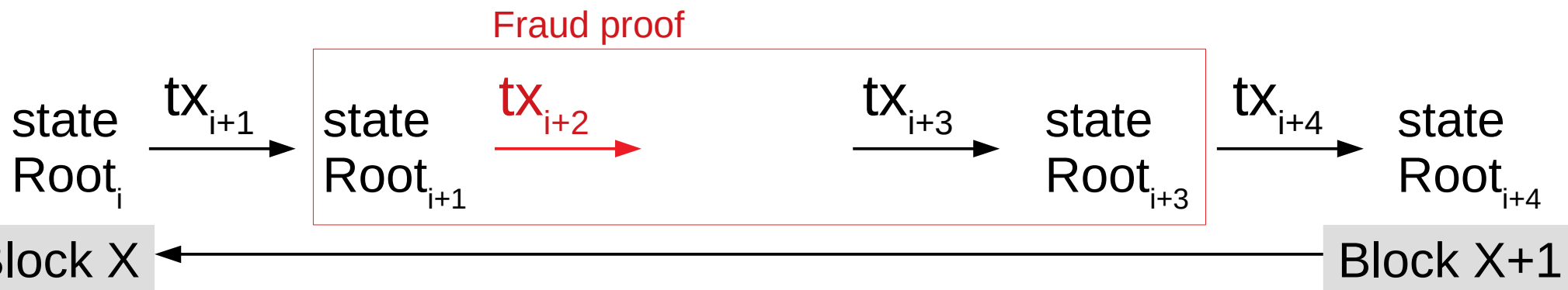
$\text{rootTransition}(\text{stateRoot}_{i+1}, \text{tx}_{i+1}, \text{witnesses}_{i+1}) \neq \text{stateRoot}_{i+2}$

then the fraud proof is valid.

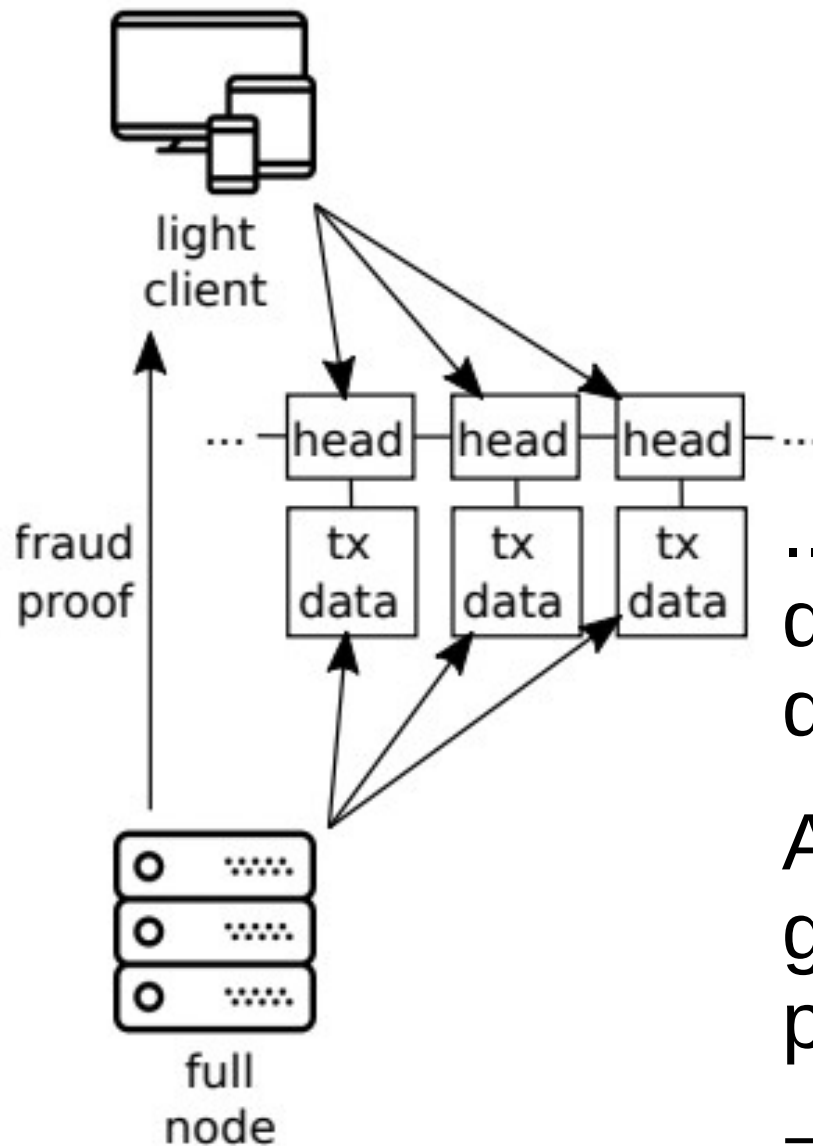


# Generalising the blockchain as a state transition system

- ▶ You don't have to include the state root after every transaction – this saves block space but the fraud proof gets bigger.



# The data availability problem



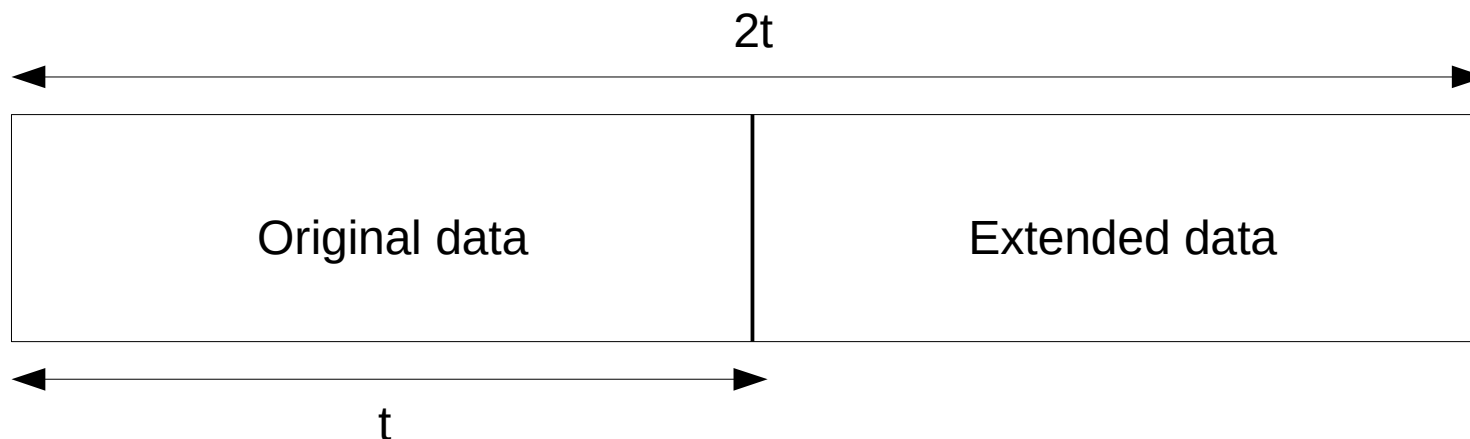
...but what if the miner doesn't release the tx data?

A: Then we can't generate a fraud proof. 🤖

= We also need a way to guarantee data availability! 15

# Erasure coding

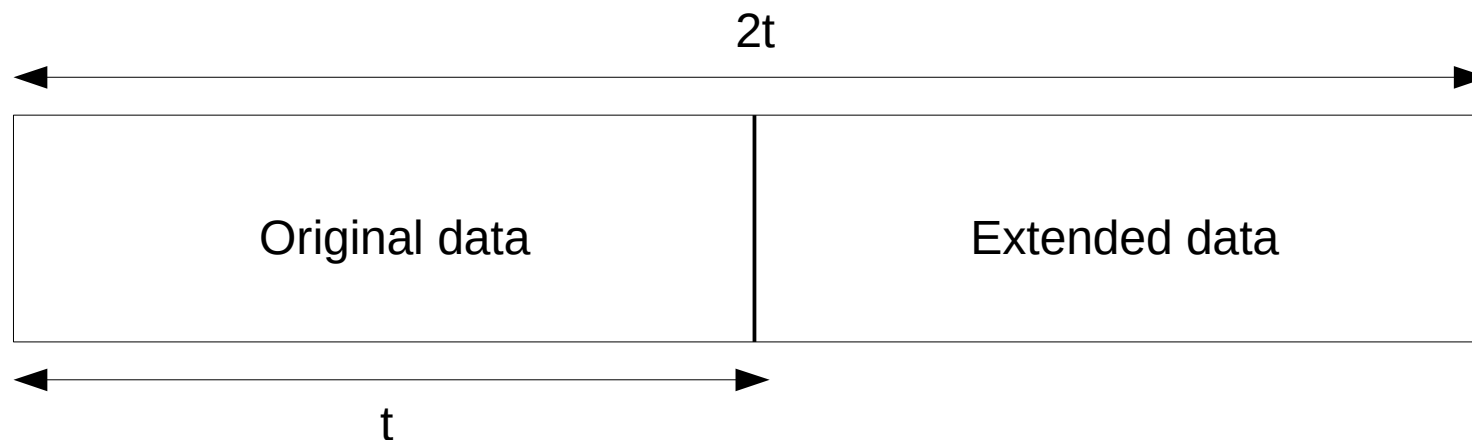
- ▶ Using erasure coding, you can extend data  $t$  pieces long to  $2t$  pieces, such that you can recover the whole data from any  $t$  pieces.





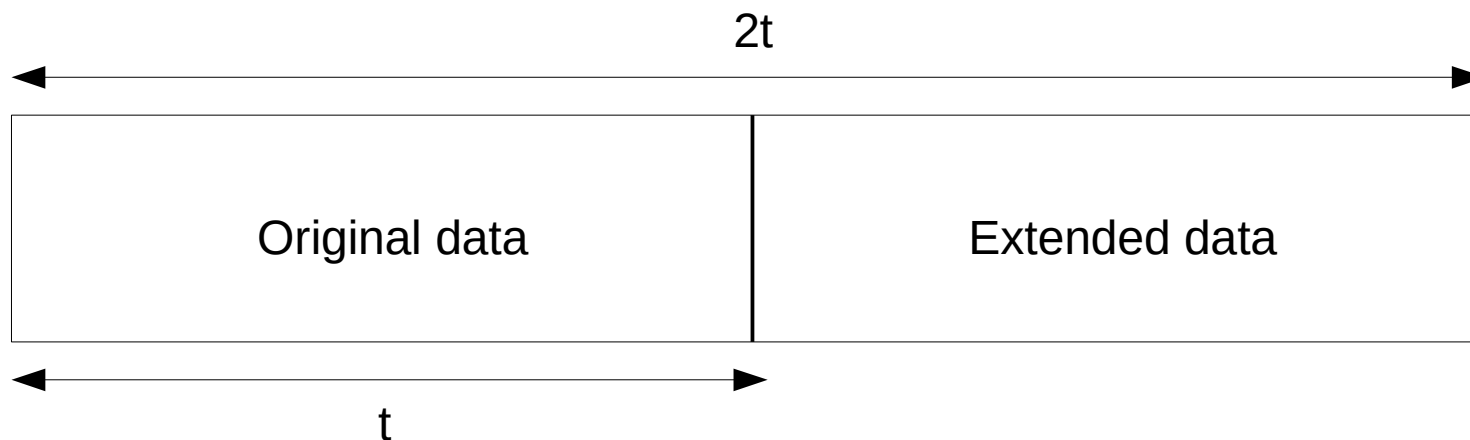
# Naive data availability scheme

- ▶ We can require miners to commit to the Merkle root of the erasure coded version of the block data. In order for a miner to hide any piece of the block, they must hide 50%.
- ▶ Thus clients can randomly sample parts of the block (with replacement), and if 50% is hidden, then there is a  $2^{-s}$  chance of landing on an unavailable piece, then the block is rejected.
- ▶ Clients gossip pieces to full nodes for recovery.



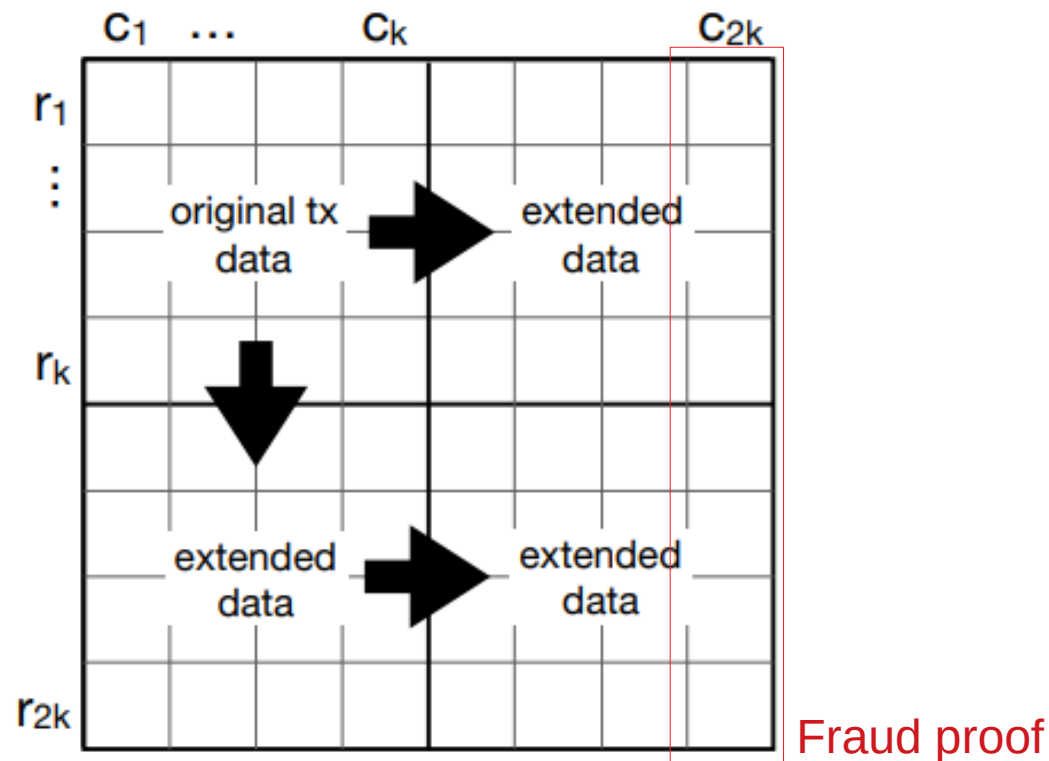
# Naive data availability scheme

- ▶ Problem: what if the miner incorrectly generates the erasure code?
  - ▶ In order to prove this, the fraud proof consists of the entire block, as clients will need to download and regenerate the erasure code to check if it's correct.
  - ▶ That's  $O(\text{blocksize})$ . Back to square one!



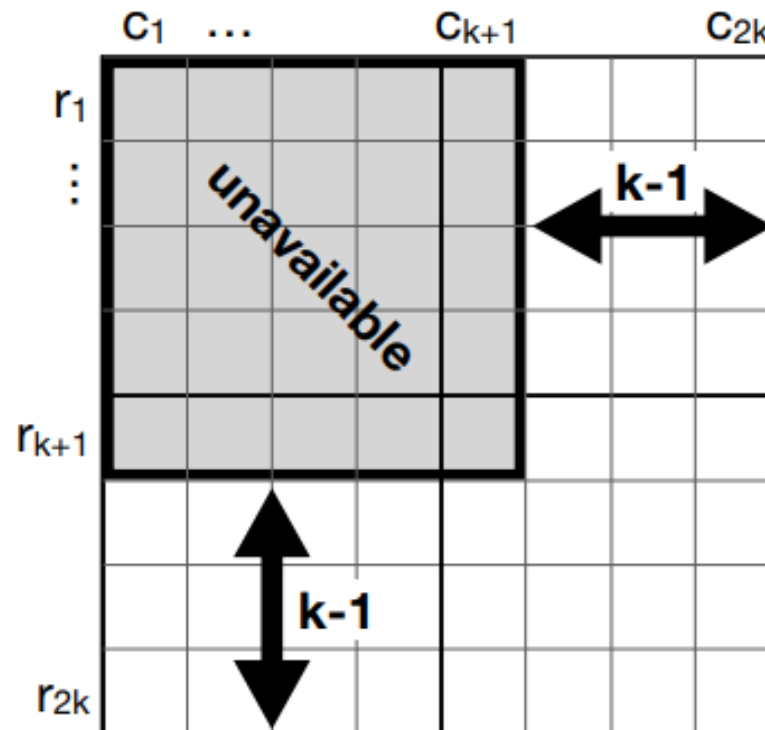
# Multidimensional coding

- ▶ We can use multidimensional coding to fix this.
- ▶ If any row or column is incorrectly generated, a fraud proof that the code is incorrectly generated is limited to that specific row or column. That's  $O(\sqrt{\text{blocksize}})$ .



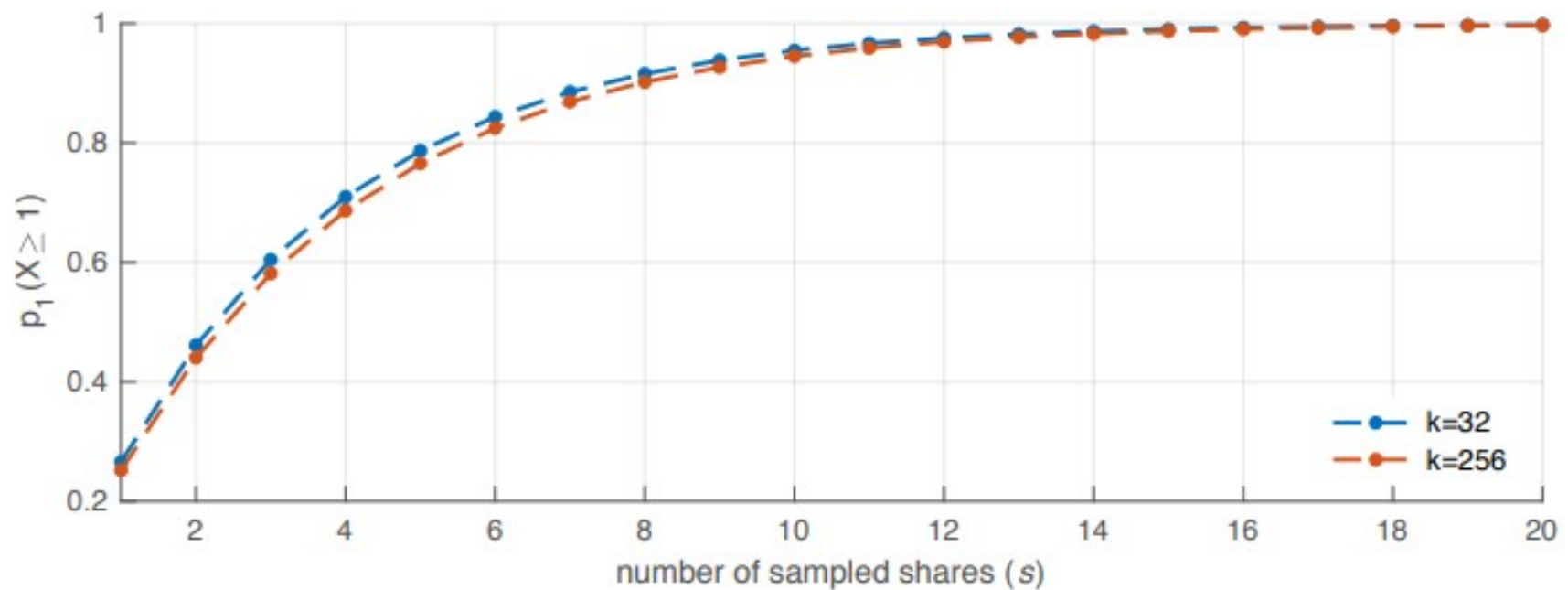
# Multidimensional coding

- ▶ Miner has to hide roughly 25% of the square to hide any pieces.



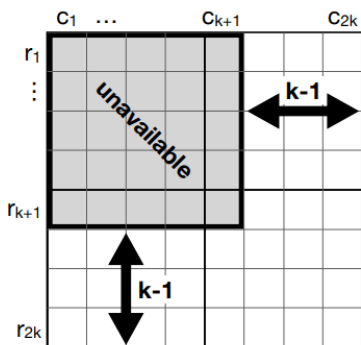
# Probability analysis

- ▶ What is the probability of a client landing on at least one available piece if the miner has hidden  $\sim 25\%$  of the square (if sampling without replacement)?
- ▶ 60% after 3 samplings; 99% after 15 samplings.



# Selective releasing of pieces

- ▶ What if a miner only releases pieces as clients ask for them?
  - ▶ Then the miner can always pass the sampling challenge of the first couple of hundred to thousand clients.
  - ▶ The exact number of how many clients can be fooled depends on how many samples they make each ( $s$ ) and how wide is the square ( $k$ ).



$p_e(Z \geq \gamma)$	$s = 2$	$s = 5$	$s = 10$	$s = 20$	$s = 50$
$k = 16$	692	277	138	69	28
$k = 32$	2805	1,122	561	280	112
$k = 64$	11,289	4,516	2,258	1,129	451
$k = 128$	>40,000	~18,000	~9,000	~4,500	1,811

# Preventing selective releasing of pieces

- ▶ We can prevent this by assuming an enhanced network model.
  - ▶ Clients send requests anonymously.
  - ▶ The order in which requests are received by the network are uniformly random (i.e. client's sampled are interleaved). For example, using a mix net.
- ▶ This would mean that a miner would have same probability of fooling all clients, including the first ones to ask for samples.
  - ▶ Because requests are unlinkable to clients; sampling challenges cannot be satisfied on a per-client basis.

# Block validity security assumptions comparison

- ▶ What additional security assumptions are necessary to only accept valid blocks?

Full nodes	SPV clients	SPV clients + fraud proofs
	+ 51% of consensus is honest	+ at least one honest full node in connected network graph + maximum network delay to receive proofs (e.g. 5 mins) + minimum number of light clients (few hundred)



# Implementation

- ▶ 2D Reed-Solomon Merkle tree data availability scheme:  
<https://github.com/musalbas/rsmt2d>
- ▶ Fraud proofs prototype:  
<https://github.com/asonnino/fraudproofs-prototype>
- ▶ Sparse Merkle tree library with support for state transition witness verification:  
<https://github.com/musalbas/smt>

# Performance: space/bandwidth

Object	Space complexity	250KB block	1MB block
State fraud proof	$O(p + p \log(d) + w \log(s) + w)$	14,090b	14,410b
Availability fraud proof	$O(d^{0.5} + d^{0.5} \log(d^{0.5}))$	5,120b	12,288b
Single sample response	$O(\text{shareSize} + \log(d))$	320b	368b
Header	$O(1)$	128b	128b
Header + axis roots	$O(d^{0.5})$	2,176b	4,224b

Table 2: Worst case space complexity and illustrative sizes for various objects for 250KB and 1MB blocks.  $p$  represents the number of transactions in a period,  $w$  represents the number of witnesses for those transactions,  $d$  is short for `dataLength`, and  $s$  is the number of key-value pairs in the state tree. For the illustrative sizes, we assume that a period consists of 10 transactions, the average transaction size is 225 bytes, and that conservatively there are  $2^{30}$  non-default nodes in the state tree.

# Performance: computation

Action	Time complexity	250KB block	1MB block
[G] State fraud proof	$O(b + p \log(d) + w)$	289.78 ms	981.88 ms
[V] State fraud proof	$O(p + p \log(d) + w)$	1.50 ms	1.50 ms
[G] Availability fraud proof	$O(d^2 + d^{0.5} \log(d^{0.5}))$	7.96ms	50.88ms
[V] Availability fraud proof	$O(d + d^{0.5} \log(d^{0.5}))$	0.05ms	0.19ms
[G] Single sample response	$O(\log(d^{0.5}))$	< 0.00001ms	< 0.00001ms
[V] Single sample response	$O(\log(d^{0.5}))$	< 0.00001ms	< 0.00001ms

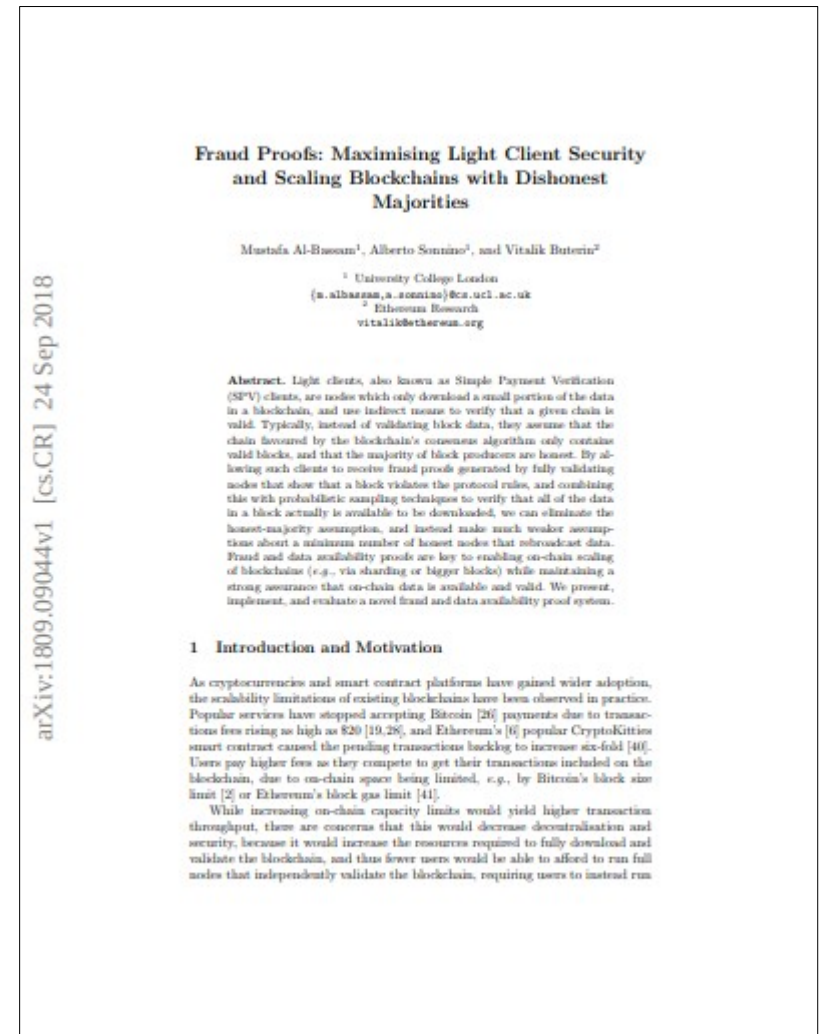
Table 3: Worst case time complexity and benchmarks for various actions for 250KB and 1MB blocks (mean over 10 repeats), where [G] means generate and [V] means verify.  $p$  represents the number of transactions in a period,  $b$  represents the number of transactions in the block,  $w$  represents the number of witnesses for those transactions,  $d$  is short for `dataLength`, and  $s$  is the number of key-value pairs in the state tree. For the benchmarks, we assume that a period consists of 10 transactions, the average transaction size is 225 bytes, and each transaction writes to one key in the state tree.

# Read the full paper (33 pages)

## ► Fraud Proofs: Maximising Light Client Security and Scaling Blockchains with Dishonest Majorities

Mustafa Al-Bassam, Alberto Sonnino, Vitalik Buterin

► <https://arxiv.org/abs/1809.09044>



# Thank you

- ▶ Questions?
- ▶ Twitter: @musalbas
- ▶ Email: [mus@musalbas.com](mailto:mus@musalbas.com)