

# Instantiating Scriptless 2P-ECDSA

Fungible 2-of-2 Multisigs for Today's Bitcoin

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# History and Motivation

- Andrew Poelstra releases work on Schnorr-based Scriptless Scripts in 2016
  - Follows up w/ construction for replacing hash-preimage challenge in LN (March 2017)
  - Ensures payment information is randomized at every hop
    - Increases privacy
    - Prevents fee-siphoning mentioned by Pedro
- In late 2017, Yehuda Lindell publishes efficient 2P-ECDSA signing protocol
  - Offers ability to do 2-of-2 ECDSA multisigs **without updating consensus layer**
  - Retains anonymity set of existing P2WKH wallet transactions
- April 2018, Multi-Hop Locks paper delivers formalized framework for LN hop decorrelation
  - Includes Scriptless Script construction based on 2P-ECDSA protocol
  - Shows that Schnorr and 2P-ECDSA are fully interoperable
    - Can be mixed heterogeneously on same LN path!
    - Implies that switching from ECDSA to Schnorr **won't fragment the network**

## LN gains of moving to Schnorr/ECDSA Multi-Hop Locks:

- Increased privacy for both on-chain and off-chain transactions
- Smaller transactions and fees
- *Real* proofs-of-payment (“Invoice Tunneling”)
- More extensions yet to come ;)

# Agenda

- I. 2P-ECDSA Overview**
- II. Benchmarks**
- III. Applications to Lightning**
- IV. Deployment Considerations**

# 2P-ECDSA Overview

Two participants, Alice and Bob:

- Alice has private key  $a$  and public key  $A = a*G$
- Bob has private key  $b$  and public key  $B = b*G$
- Jointly create public key  $Q = ab*G$  with private key  $ab$ , but...
  - **neither knows**  $ab$  outright, yet...
  - together they can create valid ECDSA signatures under  $Q$

Requires two algorithms:

- **KeyGen** (offline):
  - Sets up Alice and Bob for participation in online signing protocol
  - More expensive, but only executed once
- **Sign** (online):
  - Produces an ECDSA signature under  $Q$
  - 2 RTT
- Fast Secure Two-Party ECDSA Signing, Yehuda Lindell. <https://eprint.iacr.org/2017/552.pdf>
- Efficient RSA Key Generation and Threshold Paillier in the Two-Party Setting, Hazay et. al. <https://eprint.iacr.org/2011/494.pdf>
- A Generalisation, a Simplification and some Applications of Paillier's Probabilistic Public-Key System, Damgard and Jurik. <http://www.brics.dk/RS/00/45/BRICS-RS-00-45.pdf>

# 2P-ECDSA Overview (KeyGen)

- **KeyGen:**

- Alice and Bob exchange pubkeys, each provides discrete log PoK
- Alice generates a Paillier keypair  $(PSK, PPK)$ 
  - Provides ZKP that  $PPK$  is constructed properly,  $N = p_1 * p_2$
- Alice encrypts her private key under  $PPK$ , creating ciphertext  $c = Enc_{PPK}(a)$
- Alice sends  $(PPK, c)$  to Bob
  - Provides ZKP that ciphertext contains “small” value
    - i.e.,  $0 < Dec_{PSK}(c) < q$ , where  $q$  is the secp256k1 curve order
  - AND that  $c$  contains Alice’s private key,  $A = Dec_{PSK}(c) * G$
  - Lindell had to invent a new ZKP to do so!
- Bob verifies all the proofs and computes  $Q = b * A$
- Alice computes  $Q = a * B$
- Output:
  - Alice saves 2P-ECDSA private key  $(a, PSK)$  with public key  $Q = ab * G$
  - Bob saves 2P-ECDSA private key  $(b, c, PPK)$  with public key  $Q = ab * G$

## 2P-ECDSA Overview (Sign)

- Sooo why all this Paillier nonsense?
  - Can't "add" signatures and pubkeys as we can with Schnorr
  - Paillier ciphertexts exhibit partially-homomorphic properties
    - Additive:  $D(E(m_1) * E(m_2) \bmod N^2) = m_1 + m_2 \bmod N$
    - Scalar-multiplicative:  $D(E(m)^k \bmod N^2) = k * m \bmod N$
    - Both can be done **without private knowledge**
- ECDSA signature:  $(R, s)$  where  $s = k^{-1} * (H(m) + r * x)$  and  $r = x\text{-coord}(R = k * G)$
- **Sign:**
  - Alice and Bob exchanges nonces w/ discrete log PoK,  $K_a = k_a * G$  and  $K_b = k_b * G$
  - Bob encrypts  $c_1 = \text{Enc}_{PPK}(k_b^{-1} * H(m))$  and  $v = k_b^{-1} * r * b$  where  $r = x\text{-coord}(R = k_a^{-1} k_b^{-1} * G)$
  - Bob computes and sends  $c' = c_1 * c^v \bmod N^2 = \text{Enc}_{PPK}(k_b^{-1} * (H(m) + r * a * b))$  to Alice
  - Alice  $s' = \text{Dec}_{PSK}(c')$  and computes  $s'' = k_a^{-1} * s' \bmod q$
  - Sure enough,  $s'' = k_a^{-1} * k_b^{-1} * (H(m) + r * a * b)$
  - Finally, Alice sets  $s = \min(s'', q - s'' \bmod q)$  and outputs signature  $(R, s)$

# Benchmarks

	Time	Memory Allocated	Num Allocations	Num Messages
<b>KeyGen</b> <sup>[1]</sup>	1.07 s	4.99 MB	13.31 K	7
<b>Sign</b>	28.66 ms	97 KB	746	4
<b>Scriptless-Sign</b>	29.40 ms	118 KB	1.12 K	5+1

## Setup:

- 2.8 GHz Intel Core i7 16 GB 2133 MHz LPDDR3
- Single process, no network latency or serialization
- Non-interactive DLOG PoK and Proof of Paillier Paillier Key Correctness
- Interactive Paillier Range and DLog Ciphertext Proof

Golang code will be published here: <https://github.com/cfromknecht/tpec> (1.7K LOC)

Concurrent work in Rust by Gary Bennatar and Omer Shlomovits: <https://github.com/KZen-networks/multi-party-ecdsa>

- Also working on t-of-n threshold ECDSA signing!

[1] Likely to change after further refinement and optimization

# Deployment Considerations - Script Modifications

- 2P-ECDSA/Schnorr
  - Funding Outputs
    - Currently regular 2-of-2 multisigs
    - Requires 2-of-2 signature to spend
      - Cooperative closes
      - Commitment transactions
    - Replaced with P2WKH-looking output
  - HTLC Outputs
    - Uses 2-of-2 multisig in non-standard HTLC scripts
    - Two types of HTLC scripts: offered and received
    - Requires 2-of-2 sig to spend offered-timeout and received-success clauses
    - Replaced with *much* simpler HTLC script
- Scriptless 2P-ECDSA/Schnorr
  - HTLC Outputs
    - Remove payment hashes from HTLC scripts!
    - By extension, remove preimages from witnesses



# Deployment Considerations - Funding Output Scripts

	Witness	Witness Script
Regular 2-of-2 MultiSig	$OP_0 \langle a * G \text{ sig} \rangle \langle b * G \text{ sig} \rangle$	$OP_2 \langle a * G \text{ pubkey} \rangle \langle b * G \text{ pubkey} \rangle OP_2 OP\_CHECKMULTISIG$
Schnorr 2-of-2 MultiSig	$\langle (a+b) * G \text{ sig} \rangle$	$\langle (a+b) * G \text{ pubkey} \rangle OP\_CHECK\_SCHNORR\_SIG$
2P-ECDSA 2-of-2 MultiSig	$\langle ab * G \text{ sig} \rangle$	$\langle ab * G \text{ pubkey} \rangle OP\_CHECKSIG$
P2WKH	$\langle a * G \text{ sig} \rangle$	$\langle a * G \text{ pubkey} \rangle OP\_CHECKSIG$

- Witness bytes required to spend:
  - Regular 2-of-2: ~220
  - 2P-ECDSA and P2WKH: ~109
  - Schnorr: 100
- 2P-ECDSA is indistinguishable from P2WKH, increased anonymity set
  - Huge win for non-advertised channels

# Deployment Considerations - HTLC Scripts

## New Received-HTLC Witness Script

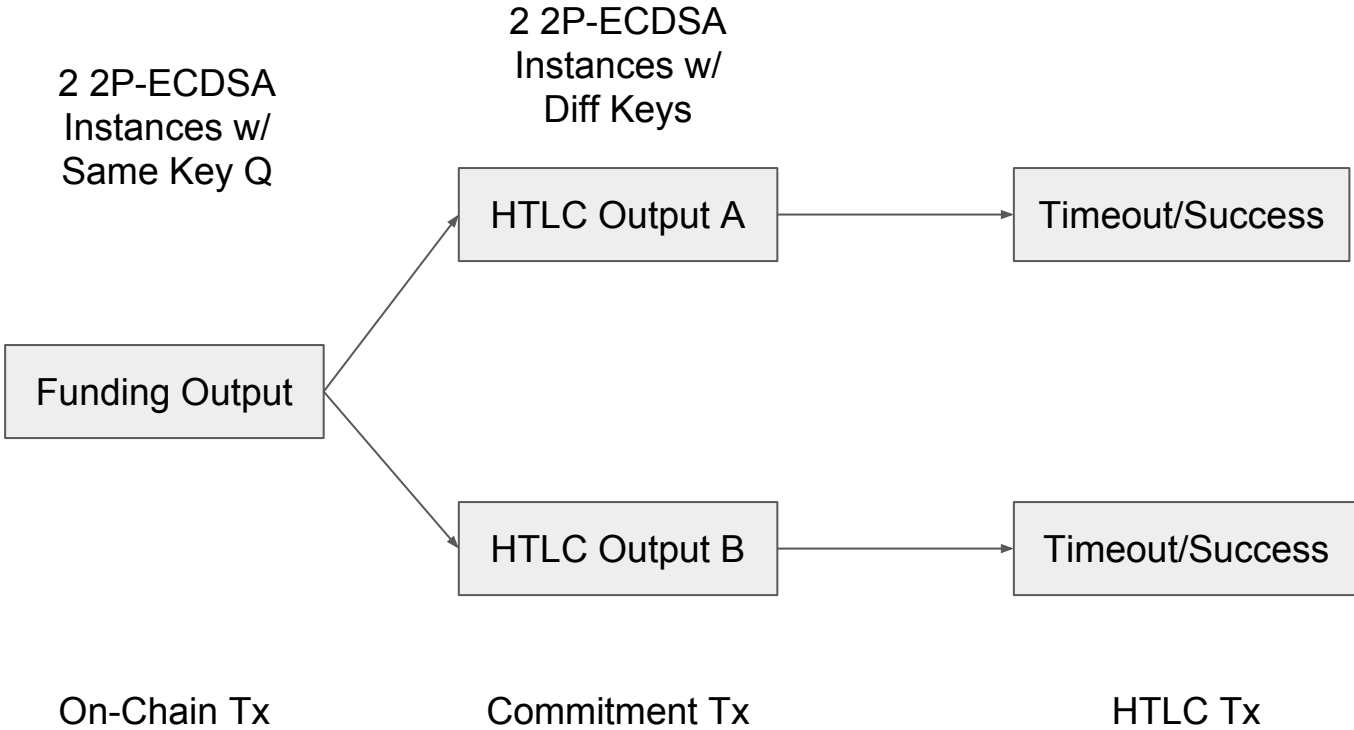
```
OP_IF
  # revocation clause
  revocationpubkey
OP_ELSE
  OP_IF
    # timeout clause
    <cltv_expiry> OP_CLTV OP_DROP
    <remote_delay_pubkey>
  OP_ELSE
    # success clause
    <2p_htlc_pubkey>
  OP_ENDIF
OP_ENDIF
OP_CHECKSIG
```

- 20% reduction in witness script size
- Improves readability immeasurably
- Reduced witness size
  - 78% for success witness
  - 30% for revocation witness
  - Timeout witness stays the same

## Current Received-HTLC Witness Script

```
# revocation clause
OP_DUP OP_HASH160
<RIPEMD160 (SHA256 (revocationpubkey))> OP_EQUAL
OP_IF
  OP_CHECKSIG
OP_ELSE
  <remote_htlcpubkey> OP_SWAP OP_SIZE 32 OP_EQUAL
  OP_IF
    # success clause
    OP_HASH160 <RIPEMD160 (payment_hash)>
  OP_EQUALVERIFY
  2 OP_SWAP <local_htlcpubkey> 2 OP_CHECKMULTISIG
  OP_ELSE
    # timeout clause
    OP_DROP <cltv_expiry> OP_CLTV OP_DROP
    OP_CHECKSIG
  OP_ENDIF
OP_ENDIF
```

# Deployment Considerations - 2P-ECDSA Instances



# Deployment Considerations - Onion Packets

## BOLT 04 Onion Packet Structure



### Current per-hop payload (32 bytes)

```
[8:short_channel_id]
[8:amt_to_forward]
[4:outgoing_cltv_value]
[12:padding]
```

Total: 1300 bytes

### MHL per-hop payload (161 bytes)

```
[8:short_channel_id]
[8:amt_to_forward]
[4:outgoing_cltv_value]
[33:incoming_lock_pubkey]
[64:incoming_lock_dlog_pok]
[32:hop_lock_secret]
[12:padding]
```

Total: 3880 bytes

- Performance is dominated by asymmetric operations
  - Used to derive per-hop ephemeral keys and blinding factors
  - But, scales linearly in the number of hops!
- Increased message size likely have marginal impact on construction/decryption

**Thank You!**

